## Chapter 10

## Item Analysis and Review

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### 10.1 Overview

An important stage in creating the PIRLS 2006 achievement scale was an extensive review of the item statistics prior to item response theory (IRT) scaling. This review was conducted by the TIMSS \& PIRLS International Study Center and involved evaluating the psychometric characteristics of each item within and across the participating countries. The purpose of this review was to ensure the quality of PIRLS achievement data by screening items for unusual item characteristics that could be attributed to an error, identifying the source, and rectifying the problem. For example, an item with low discrimination in one country atypical of the item's discrimination power in general may indicate a translation or printing problem. Also, for the trend items, item statistics were compared between 2001 and 2006.

In the few cases where country-level problems were identified, the TIMSS \& PIRLS International Study Center consulted translation verification materials, checked printed booklets, and contacted National Research Coordinators (NRCs) to determine the source of the problem. When necessary, the item was removed from the international database for that country. This chapter describes the review process and the basic item statistics that were employed, using examples from the assessment.

### 10.2 Statistics for Item Analysis

As a first step, the TIMSS \& PIRLS International Study Center created data almanacs containing the basic statistics for each achievement item. Exhibits 10.1 and 10.2 show examples of these statistics for a multiple-choice and constructedresponse item, respectively. As these exhibits show, statistics were computed for each country individually, as well as on average internationally. The five Canadian provinces, listed below the international average row, were not included in the calculation of the international average.

For each item, almanacs include the number of students who were administered the item, item difficulty, item discrimination, and the percentage of boys and girls who responded correctly. For multiple-choice items, the percentage of students who chose each option and the percentage of students who omitted or did not reach the item was computed. In addition, the pointbiserial correlation between each option and the total score was calculated. For constructed-response items, the percentage of students at each score level, the difficulty and discrimination for each score level (items could have up to 3 points), the number of responses that were double-scored, and the reliability between the two scorers were calculated. More detailed descriptions of these statistics are provided below.

- N : The number of students who were administered the item. If a student did not reach the item, it was considered not administered during item analysis. ${ }^{1}$
- Diff: Item difficulty, calculated as the percentage of students providing a correct response to the item. For constructed-response items worth more than one point, this is the students' average score as a percentage of the maximum score points for the item. Items that were not reached by the students were treated as not administered when computing this statistic.
- Disc: Item discrimination, calculated as the correlation between a correct response to the item and the total score on all items in the test booklet. ${ }^{2}$ For constructed-response items worth more than one point, the correlation between the number of score points and total score was used. Items exhibiting good measurement properties should have a moderately positive correlation.


## Exhibit 10.1 International Item Statistics for a Multiple-choice Item

Progress in International Reading Literacy Study - PIRLS 2006 Assessment Results
International Item Statistics (Unweighted) -4th Grade
For Internal Review Only: DO NOT CITE OR CIRCULATE
Acquire and Use Information: Focus on and Retrieve Explicitly Stated Information and Ideas (Searching for Food)
Label: How do other ants from nest find food too (R021S04M - So4)
Item Type $=\mathrm{MC}$ Key $=\mathrm{C}$


[^0]Exhibit 10.2 International Item Statistics for a Constructed-response Item
Progress in International Reading Literacy Study -
International Item Statistics (Unweighted) - 4th Gr
For Internal Review Only: DO NOT CITE OR CIRCULATE
Acquire and Use Information: Make Straightforward Inferences (Antarctica)
Label: Ways penguins keep warm (R011A07C - A07) Item Type $=\mathrm{CR} \quad$ Key $=\mathrm{X}$


$$
\begin{aligned}
& \text { Keys: Diff = Percent Correct Score; Disc= Item Discrimination; Pct_0... } 3=\text { Percent Obtaining Score Level; Pct_OM, NR= Percent Omitted, Not Reached; } \\
& \text { PB_0...2= Point Biserial for Score Level; PB_OM= Point Biserial for Omitted; RDIFF= Rasch Difficulty; }
\end{aligned}
$$

- Pct_A, Pct_B, Pct_C, Pct_D: Used for multiple-choice items only, each column indicates the percentage of students choosing the particular response option (A, B, C, or D). Students who did not reach the item were excluded from the denominator for these calculations.
- Pct_0, Pct_1, Pct_2, Pct_3: Used for constructed-response items only, each column indicates the percentage of students earning the particular number of score points ( $0,1,2$, or 3 ) for that item. Students who did not reach the item were excluded from the denominator for these calculations.
- Pct_In: Used for multiple-choice items only, this column indicates the percentage of students who provided an invalid response to the item. A typical invalid response was a student selecting multiple response options for an item.
- Pct_OM: This column indicates the percentage of students who reached the item but did not provide a response. Students who did not reach the item were excluded from the denominator when calculating this statistic.
- Pct_NR: This column indicates the percentage of students who did not reach the item. An item was considered not reached if the student did not respond to any subsequent items in the test booklet, and the previous item was omitted.
- PB_A, PB_B, PB_C, PB_D: Used for multiple-choice items only, each column indicates the point-biserial correlation between the particular option (A, B, C, or D) and the total score. Items with good psychometric properties have near-zero or negative correlation coefficients for the incorrect options and a moderately positive correlation coefficient for the correct option.
- PB_0, PB_1, PB_2, PB_3: Used for constructed-response items only, each column indicates the correlation between the particular score level ( $0,1,2$, or 3 ) and the total score. Items with good psychometric properties should increase with each score level.
- PB_In: Used for multiple-choice items only, this column indicates the correlation between an invalid response to the item (i.e., selecting multiple response options) and total score. For an item with good psychometric properties, this should be negative or near zero.
- PB_OM: This column indicates the correlation between a binary variable indicating an omitted response to the item and the total score. For an item with good psychometric properties, this should be negative or near zero.
- RDIFF: This is an estimate of the item's difficulty based on a Rasch oneparameter IRT model. The difficulty estimate is expressed in logits (with a positive logit indicating a difficult item) and was scaled so that the average Rasch item difficulty was zero within each country.
- Avg. Score Girls/Boys: These columns indicate the average difficulty for the item separately for boys and girls.
- Reliability Cases: To provide a measure of the scoring reliability of constructed-response items, those items in approximately one quarter of the test booklets were scored by two independent scorers in each country. This column indicates the number of responses that were double-scored for an item.
- Reliability Score: Used for constructed-response items only, this column indicates the percentage of exact agreement between two independent scorers.
As an aid during the review process, the almanacs also include a series of "flags" to highlight conditions that may warrant a closer look. While not all flags necessarily signify a faulty item, they draw attention to potential problems.

The following conditions are flagged:

- Difficulty levels for the item are significantly different for boys and girls;
- Item difficulty is less than chance (e.g., $25 \%$ for multiple-choice items);
- Item difficulty exceeds 95 percent;
- Item discrimination (i.e., the point-biserial for the correct option) is less than 0.2 ;
- Rasch difficulty estimate is below the average of all items;
- Rasch difficulty estimate is above the average of all items;
- For multiple choice items, a greater percentage of students chose the incorrect response than the percentage of students who chose the correct option, or the point-biserial correlation for one or more of the distracters exceeds zero;
- Less than 10 percent of students chose one or more of the distracters (for multiple-choice items) or earned one or more of the score levels (for constructed-response items);
- Scoring reliability is less than 80 percent; and
- Students with lower total scores are more likely to answer an item correctly than students with higher total scores.

In addition to item-level statistics, the TIMSS \& PIRLS International Study Center also examined descriptive statistics for each test block as a whole to gain a sense of the overall performance of the items associated with each passage. These statistics included the number of students who were administered the block, the minimum, maximum, and average number of items students answered correctly, the standard deviation, the percent correct overall and, for boys and girls separately, the minimum, maximum, and average point-biserial correlation across the items, and the Cronbach's alpha reliability coefficient for the block. Each of these was calculated for individual countries and on average internationally.

Eleven countries and the five Canadian provinces administered the assessment in more than one language. ${ }^{3}$ In these cases, an additional step was taken to examine item statistics for each language group. Due to the fact that some language groups make up a small proportion of the overall sample in a country, problems with a particular language within a country may not have been evident when the languages are combined, and may indicate a translation error for that language. The same process and statistics that were described above were used for this step.

### 10.3 Examining Item-by-Country Interactions

While it is reasonable to expect country performance to vary somewhat across items, countries with high average performance should generally perform well on each of the items, and countries with lower overall performance should do less well on individual items. When this pattern is not followed (i.e., a highperforming country does poorly on a particular item), this is called an item-by-country interaction. If this interaction is large, it could indicate a problem with the item that should be investigated and addressed.

To easily detect item-by-country interactions, the TIMSS \& PIRLS International Study Center created plots that graphically display the Rasch difficulties for each item. Exhibit 10.3 displays the 95 percent confidence interval
for the national average Rasch difficulty estimate. The limits for the confidence intervals were computed as follows:

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\begin{aligned}
& \text { Upper Limit }=1-\frac{e^{\text {RDIFF }_{i k}+S E_{\text {RDIFF }_{i k}} \mathrm{x} Z_{b}}}{1+e^{\text {RDIFF }_{i k}+S E_{\text {RDIF }_{i k}} \times Z_{b}}} \\
& \text { Lower Limit }=1-\frac{e^{\text {RDIFF }_{i k}-S E_{\text {RDIFF }_{i k}} \times Z_{b}}}{1+e^{\text {RDIFF }_{i k}-S E_{\text {RDIFF }_{i k}} \times Z_{b}}}
\end{aligned}
$$

where RDIFF $_{i k}$ is the Rasch difficulty of item $k$ within country $i, S E_{\text {RDIFFik }}$ is the standard error of the difficulty of item $k$ in country $i$, and $Z_{b}$ is the critical value from the $Z$ distribution, corrected for multiple comparisons using the Bonferroni procedure. With the international average Rasch difficulty scaled to zero as a reference point, countries with a positive difference between the national and international Rasch difficulty found the item easier, and countries with a negative difference found the item more difficult.

### 10.4 Trend Item Analysis

Because an important part of the PIRLS 2006 assessment was the measuring trends across cycles, there was an additional stage of the review process to ensure that the trend items had similar characteristics in both cycles (i.e., an item that was relatively easy in 2001 should be relatively easy in 2006). The comparison between cycles was made in a number of ways. For each trend country, almanacs of item statistics displayed the percentage of students within each score category (or response option, for multiple-choice items) for each cycle, as well as the difficulty of the item and the percent correct by gender. While some changes were anticipated as countries' overall reading achievement may have improved or declined, items were noted if the percent correct changed by more than 15 percent for a particular country.

The TIMSS and PIRLS International Study Center used two different graphical displays to examine the differences between item difficulties in 2001 to 2006. The first of these, shown in Exhibit 10.4, displayed the difference in Rasch difficulty estimates (in logits) between the two assessment cycles. A positive difference indicates that the item was relatively easier in a country in 2006, and a negative difference indicates that an item was relatively more difficult. The second shows a country's performance on all trend items simultaneously.

Exhibit 10.3 Sample Plot of Item-by-Country Interactions for a PIRLS 2006 Item


Individually for each country, a scatterplot graphed the Rasch difficulty of each item in 2001 against the difficulty for that item in 2006. Where there are no differences between the difficulties in 2001 and 2006, the data points will align on or near the diagonal indicating a one-to-one correlation between cycles.

These graphs were used in conjunction with one another to detect items that performed differently in the two cycles. When such items were found, the source of the difference was investigated using booklets from both cycles, translation verifier's comments, national adaptation forms, and trend scoring reliability data.

### 10.5 Scoring Reliability for Constructed-response Items

Almost two thirds of the score points in the PIRLS 2006 assessment were from constructed-response items. In order to include these types of items in the assessment, it is essential that they are scored reliably within and across countries. In other words, a particular student response should receive the same score, regardless of the scorer. To ensure that this was the case, specific scoring guides were created for each constructed-response item that provided descriptions of each score level and sample student responses. Countries received extensive training in the application of each of these guides, using genuine student responses as examples and practice materials. Procedures for organizing and monitoring the scoring sessions were provided in the PIRLS 2006 Survey Operations Procedures Unit 4 (TIMSS \& PIRLS International Study Center, 2005). In addition to this training, countries were required to provide several types of scoring reliability data to document the consistency with which the scoring guides were applied. These are described in the following sections.

### 10.5.1 Within-country Scoring Reliability

This first type of scoring reliability data documented the extent to which items were scored consistently within each country. For each constructed-response item, 200 randomly selected student responses were independently marked by two scorers in the country. The percent agreement between these scorers was included in the item almanacs described above and examined as part of the review process. During this review, items were noted for further examination if agreement for a particular country fell below 70 percent. On average, the exact percent agreement across items was very high at 93 percent. All countries had an average percent of exact agreement above 81 percent. The average and range of these percentages is presented in Exhibit 10.6.

Exhibit 10.4 Sample Plot of Difference in Rasch Difficulties for a PIRLS 2006 Item


Exhibit 10.5 Sample Plot of Rasch Difficulties by Country for a PIRLS 2006 Item


Exhibit 10.6 PIRLS 2006 Within-country Constructed-response Scoring Reliability Data

| Countries | Average of Percent Exact Agreement Across Items | Range of Percent Exact Agreement |  |
| :---: | :---: | :---: | :---: |
|  |  | Minimum | Maximum |
| Austria | 95 | 80 | 100 |
| Belgium (Flemish) | 90 | 73 | 99 |
| Belgium (French) | 97 | 90 | 100 |
| Bulgaria | 98 | 94 | 100 |
| Canada, Alberta | 91 | 67 | 100 |
| Canada, British Columbia | 92 | 70 | 100 |
| Canada, Nova Scotia | 93 | 84 | 100 |
| Canada, Ontario | 94 | 80 | 100 |
| Canada, Quebec | 95 | 87 | 100 |
| Chinese Taipei | 95 | 78 | 100 |
| Denmark | 97 | 90 | 100 |
| England | 98 | 93 | 100 |
| France | 89 | 69 | 100 |
| Georgia | 85 | 65 | 98 |
| Germany | 89 | 76 | 99 |
| Hong Kong SAR | 96 | 85 | 100 |
| Hungary | 98 | 89 | 100 |
| Iceland | 95 | 88 | 99 |
| Indonesia | 95 | 76 | 100 |
| Iran, Islamic Rep. of | 93 | 83 | 99 |
| Israel | 91 | 80 | 98 |
| Italy | 95 | 85 | 100 |
| Kuwait | 86 | 80 | 95 |
| Latvia | 90 | 78 | 100 |
| Lithuania | 97 | 91 | 100 |
| Luxembourg | 94 | 82 | 100 |
| Macedonia, Rep. of | 88 | 78 | 96 |
| Moldova, Rep. of | 99 | 97 | 100 |
| Morocco | 89 | 71 | 97 |
| Netherlands | 99 | 93 | 100 |
| New Zealand | 93 | 80 | 98 |
| Norway | 83 | 66 | 97 |
| Poland | 97 | 93 | 100 |
| Qatar | 97 | 93 | 99 |
| Romania | 99 | 96 | 100 |
| Russian Federation | 99 | 97 | 100 |
| Scotland | 97 | 89 | 100 |
| Singapore | 98 | 94 | 100 |
| Slovak Republic | 96 | 88 | 100 |
| Slovenia | 98 | 92 | 100 |
| South Africa | 82 | 63 | 92 |
| Spain | 81 | 61 | 96 |
| Sweden | 92 | 72 | 100 |
| Trinidad and Tobago | 93 | 71 | 100 |
| United States | 93 | 82 | 100 |
|  |  |  |  |
| International Avg. | 93 | 82 | 99 |

### 10.5.2 Cross-country Scoring Reliability

It also was important to document the consistency of scoring across countries. To accomplish this goal, the TIMSS \& PIRLS International Study Center collected 200 student responses to each of the 23 constructed-response items from four assessment blocks, for a total of 4,600 student responses. Due to the wide range of languages used in PIRLS 2006 and the logistic issues this presents for cross-country scoring, responses were only collected from participants that administered the assessment in English (the Canadian province of Ontario, England, New Zealand, Scotland, Singapore, South Africa, and the United States). These responses were scanned by the IEA Data Processing and Research Center (DPC) and provided to each country in a software program that facilitated the scoring process.

Countries were asked to provide at least two scorers who were proficient in English to score this set of responses, following the main scoring activities. Each student response was scored by 62 scorers from across the countries, giving a total of 1,891 comparisons for each student response to each item, and 378,200 total comparisons across the set of 200 responses per item. ${ }^{4}$ Exhibit 10.7 shows the percentage of exact agreement for each item. On average, there was 87 percent agreement, with variation across the individual items.

Exhibit 10.7 PIRLS 2006 Cross-country Constructed-response Scoring Reliability

| Purpose | Item Label | Total Valid Comparisons | Exact Percent Agreement |
| :---: | :---: | :---: | :---: |
| Literary Experience | Flowers F06C | 377504 | 91\% |
|  | Flowers F07C | 377957 | 80\% |
|  | Flowers F08C | 375960 | 92\% |
|  | Flowers F09C | 378078 | 93\% |
|  | Flowers F10C | 376869 | 97\% |
|  | Flowers F12C | 375684 | 63\% |
|  | Unbelievable Night U05C | 377224 | 99\% |
|  | Unbelievable Night U06C | 377385 | 93\% |
|  | Unbelievable Night U08C | 378078 | 76\% |
|  | Unbelievable Night U10C | 377453 | 96\% |
|  | Unbelievable Night U12C | 377302 | 87\% |
| uо!̣ешлоృи৷ әsก pue әı!nbכヲ | Antartica A01C | 378200 | 95\% |
|  | Antartica A03C | 378139 | 98\% |
|  | Antartica A04C | 377542 | 89\% |
|  | Antartica A07C | 378139 | 88\% |
|  | Antartica A08C | 377722 | 80\% |
|  | Antartica A09C | 377370 | 83\% |
|  | Antartica A11C | 377363 | 81\% |
|  | Day Hiking N02C | 377897 | 91\% |
|  | Day Hiking N03C | 378139 | 94\% |
|  | Day Hiking N08C | 376927 | 92\% |
|  | Day Hiking N11C | 377773 | 77\% |
|  | Day Hiking N12C | 330146 | 76\% |
|  | Average Percent Agreement |  | 87\% |

### 10.5.3 Trend Scoring Reliability

Extensive efforts were made to ensure that constructed-response items were scored consistently across testing cycles. In preparation for this, the IEA DPC scanned 200 student responses to each of the 26 trend constructed-response items from the PIRLS 2001 reliability booklet samples and provided the responses, along with the original scores from 2001, in a scoring software program. ${ }^{5}$ As part of the scoring training activities, at least two scorers in each trend country were asked to score the set of student responses for each item from the four trend blocks, for a total of 5,200 student responses. After scoring half of these responses, scorers used the software to compare their scores to one

[^1]another, as well as to the original score given in 2001. If agreement for any item fell below 85 percent, retraining was required and the responses for that item were rescored. Exhibit 10.8 shows the results of the trend scoring reliability task. Overall, the percent agreement across the trend constructed-response items was high-90 percent on average across countries.

## Exhibit 10.8 PIRLS 2006 Trend Scoring Reliability (2001-2006) for the Constructed-response Items

| Countries | Average Percent Exact Agreement Across Items |
| :---: | :---: |
| Canada, Ontario | - |
| Canada, Quebec | - |
| England | 89 |
| France | 90 |
| Germany | 88 |
| Hong Kong SAR | 93 |
| Hungary | 91 |
| Iceland | - |
| Iran, Islamic Rep. of | 92 |
| Israel | 96 |
| Italy | 91 |
| Latvia | 84 |
| Lithuania | 92 |
| Macedonia, Rep. of | 81 |
| Moldova, Rep. of | - |
| Morocco | - |
| Netherlands | 93 |
| New Zealand | 90 |
| Norway | 90 |
| Romania | - |
| Russian Federation | - |
| Scotland | 88 |
| Singapore | 88 |
| Slovak Republic | 92 |
| Slovenia | - |
| Sweden | 89 |
| United States | 93 |
| International Avg. | 90 |

A dash (-) indicates data are not available.

### 10.6 Item Review Procedures

Using the range of techniques described in the previous sections, the TIMSS \& PIRLS International Study Center reviewed the performance of each item within every participating country to ensure that the results were comparable internationally. In particular, items with the following problems were considered for possible deletion from the international database:

- An error was detected in the translation of the item that was not fixed before test administration;
- Data checking revealed a multiple-choice item with more or fewer options than the international version;
- The item analysis showed the item to have a negative biserial, or, for items with more than one score point, point biserials that did not increase with each score level;
- The item-by-country interaction results showed a very large interaction for a particular country;
- For constructed-response items, the within-country scoring reliability data showed an agreement of less than 70 percent; and
- For trend items, an item performed substantially differently in 2006 compared to 2001.
In cases where a potential problem was detected, test booklets (including PIRLS 2001 booklets, if necessary), and documentation from the translation verification and national adaptation process were reviewed. Additionally, the NRC was consulted for clarification or confirmation of translation, printing, or scoring problems. Of the 126 items used in the assessment, only one item was removed from the international database for all countries. In only three countries were one or two additional items problematic for international comparisons. The main cause of errors in items was translation or printing errors. A list of deleted and recoded items is provided in Appendix C.


## References

TIMSS \& PIRLS International Study Center. (2005). Survey operations procedures unit 4: Scoring the PIRLS 2006 assessment. Chestnut Hill, MA: Boston College.


[^0]:    $\begin{aligned} \text { Keys: } & \text { Diff= Percent Correct Score; Disc= Item Discrimination; Pct_A...D= Percent Choosing Each Option; Pct_In, OM, NR= Percent Invalid, Omitted, Not Reached; } \\ & \text { PB_A...D }=\text { Point Biserial for Each Option; PB_OM= Point Biserial for Omitted; RDIFF= Rasch Difficulty }\end{aligned}$

[^1]:    5 A number of participants were unable to complete the trend scoring reliability task because of software difficulties or because it was not possible to scan their 2001 students booklets.

