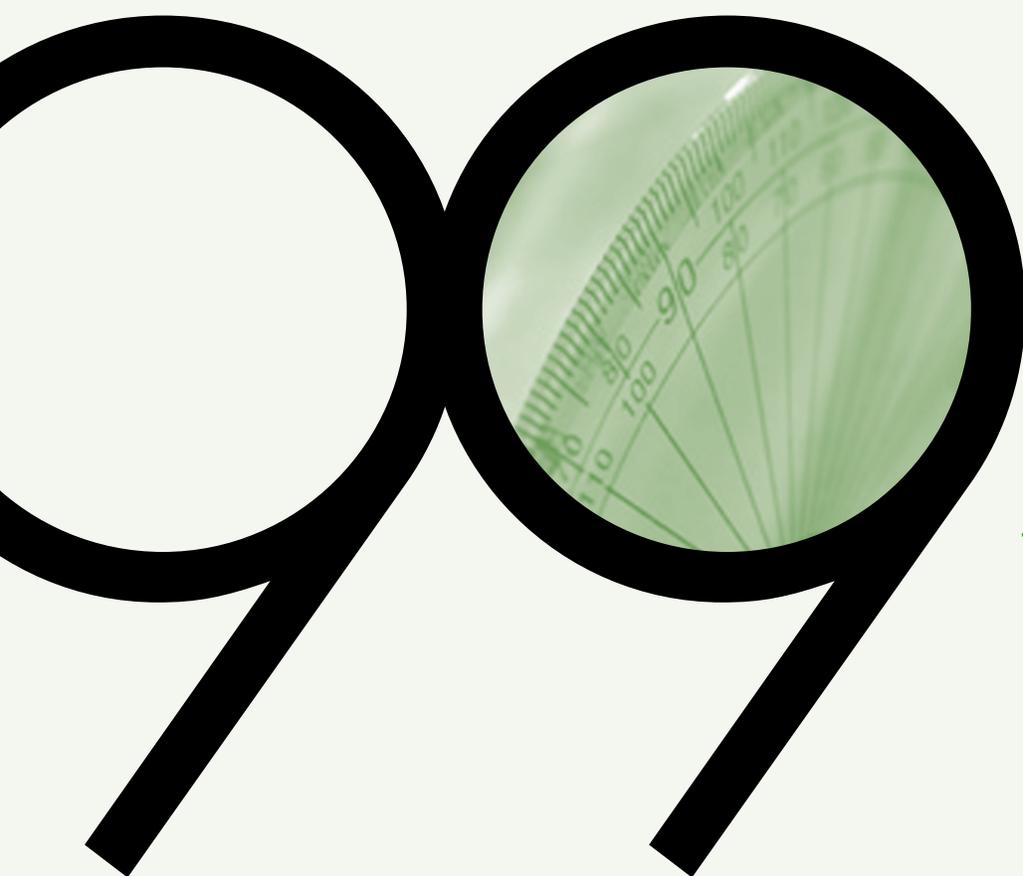


TIMSS 1999

International Mathematics Report

Findings from IEA's Repeat of the Third International Mathematics
and Science Study at the Eighth Grade



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The International Study Center
Boston College
Lynch School of Education

The International Association
for the Evaluation of
Educational Achievement

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CONTENTS

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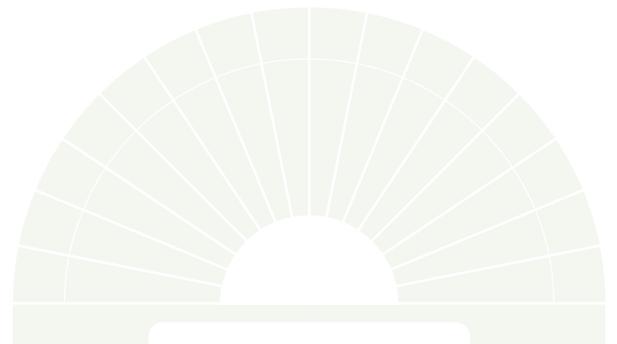
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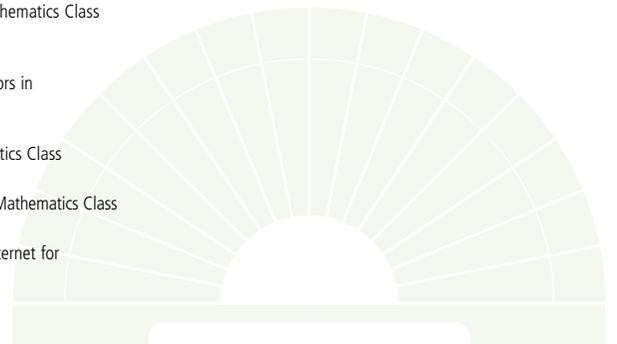
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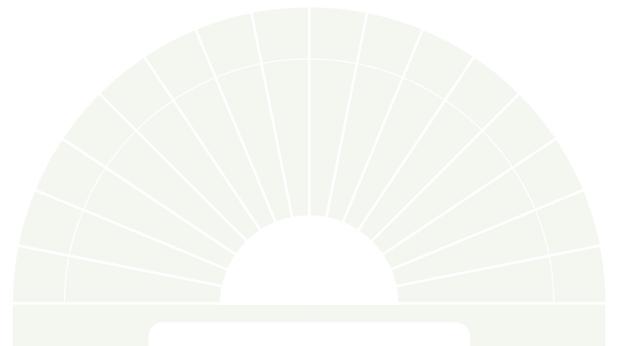
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